

Heat and Mass Transfer (DI05019071)

Complete Lecture Deck

Milav Dabgar

Lecturer, GP Palanpur

July 23, 2026

Numerical examples on Heat Exchangers (Part 2)

- Course: Heat and Mass Transfer (DI05019071)
- Unit 4: Heat exchanger
- Lecture 40: Numerical examples (NTU Method & Cross-Flow)

Lecture Agenda

- 1. When to use LMTD vs. NTU Method
- 2. Recap of Effectiveness-NTU Formulas
- 3. Example 3: Performance Prediction (NTU Method)
- 4. Recap of Multipass Correction Factor (F)
- 5. Example 4: Shell and Tube Exchanger with ' F ' Factor

LMTD vs. Effectiveness-NTU Method

- LMTD Method is best for SIZING problems:
 - - You know inlet and outlet temperatures.
 - - You need to find the required Surface Area (A).
 -
- Effectiveness-NTU Method is best for RATING/PERFORMANCE problems:
 - - You know the Surface Area (A) and inlet temperatures.
 - - You need to predict outlet temperatures and Heat Transfer Rate (Q).

Recap: Effectiveness-NTU Formulas

- Heat Capacity Rates: $C_h = m_h * C_{p,h}$, $C_c = m_c * C_{p,c}$
- Identify C_{min} (the smaller of C_h and C_c) and C_{max} .
- Capacity Ratio: $c = C_{min} / C_{max}$
- Maximum possible heat transfer: $Q_{max} = C_{min} * (T_{h,in} - T_{c,in})$
- Number of Transfer Units (NTU) = $(U * A) / C_{min}$
- Effectiveness (ϵ) = Q_{actual} / Q_{max}
- ϵ is found from charts or formulas based on NTU, c , and flow arrangement.

Example 3: Problem Statement (NTU Method)

- A counter-flow heat exchanger has a surface area of 10 m^2 and $U = 200 \text{ W/m}^2\cdot\text{K}$.
- Hot fluid ($C_p = 2.0 \text{ kJ/kg}\cdot\text{K}$) enters at 120°C at 1.0 kg/s .
- Cold fluid ($C_p = 4.18 \text{ kJ/kg}\cdot\text{K}$) enters at 20°C at 0.5 kg/s .
- Find: The rate of heat transfer and the outlet temperatures.

Example 3: Capacity Rates and NTU

- Step 1: Calculate Capacity Rates
- $C_h = 1.0 \text{ kg/s} * 2000 \text{ J/kg.K} = 2000 \text{ W/K}$
- $C_c = 0.5 \text{ kg/s} * 4180 \text{ J/kg.K} = 2090 \text{ W/K}$
- Therefore, $C_{\min} = C_h = 2000 \text{ W/K}$.
- Capacity ratio (c) = $C_{\min} / C_{\max} = 2000 / 2090 = 0.957$
-
- Step 2: Calculate NTU
- $NTU = (U * A) / C_{\min} = (200 * 10) / 2000 = 2000 / 2000 = 1.0$

Example 3: Effectiveness and Q_{actual}

- Step 3: Find Effectiveness (ε) for Counter Flow
- Formula for Counter Flow: $\varepsilon = [1 - \exp(-NTU \cdot (1 - c))] / [1 - c \cdot \exp(-NTU \cdot (1 - c))]$
- $\varepsilon = [1 - \exp(-1 \cdot (1 - 0.957))] / [1 - 0.957 \cdot \exp(-1 \cdot (1 - 0.957))]$
- $\varepsilon = [1 - \exp(-0.043)] / [1 - 0.957 \cdot \exp(-0.043)]$
- $\varepsilon = [1 - 0.9579] / [1 - 0.957(0.9579)] = 0.0421 / (1 - 0.9167) = 0.505 \text{ (or 50.5\%)}$
-
- Step 4: Calculate Q_{max} and Q_{actual}
- $Q_{\text{max}} = C_{\text{min}} \cdot (T_{\text{h,in}} - T_{\text{c,in}}) = 2000 \cdot (120 - 20) = 200,000 \text{ W} = 200 \text{ kW}$
- $Q_{\text{actual}} = \varepsilon \cdot Q_{\text{max}} = 0.505 \cdot 200 \text{ kW} = 101 \text{ kW}$

Example 3: Outlet Temperatures

- Step 5: Calculate Outlet Temperatures
- From $Q = C_h * (T_{h,in} - T_{h,out})$
- $101,000 = 2000 * (120 - T_{h,out})$
- $50.5 = 120 - T_{h,out} \Rightarrow T_{h,out} = 69.5^{\circ}\text{C}$
-
- From $Q = C_c * (T_{c,out} - T_{c,in})$
- $101,000 = 2090 * (T_{c,out} - 20)$
- $48.33 = T_{c,out} - 20 \Rightarrow T_{c,out} = 68.33^{\circ}\text{C}$

Recap: Multipass Correction Factor (F)

- For Cross-Flow and Multipass Shell-and-Tube exchangers, the flow is neither pure parallel nor pure counter-flow.
- We calculate LMTD assuming pure counter-flow, then apply a correction factor (F).
- $Q = U * A * F * \Delta T_{lm,CF}$
- F is obtained from charts based on parameters P and R:
 - - $P = (t_2 - t_1) / (T_1 - t_1)$ (Effectiveness parameter)
 - - $R = (T_1 - T_2) / (t_2 - t_1)$ (Capacity ratio parameter)

Example 4: Problem Statement (Shell & Tube)

- A 1-shell pass, 2-tube pass heat exchanger is used to heat water in tubes from 20°C to 70°C .
- Hot oil in the shell cools from 140°C to 90°C .
- Total heat transfer rate $Q = 150 \text{ kW}$.
- $U = 400 \text{ W/m}^2\cdot\text{K}$.
- Find the required surface area.

Example 4: Solution

- Step 1: Calculate LMTD for Counter Flow
- $\Delta T_1 = 140 - 70 = 70^\circ\text{C}$, $\Delta T_2 = 90 - 20 = 70^\circ\text{C}$
- Since $\Delta T_1 = \Delta T_2$, $\text{LMTD} = 70^\circ\text{C}$.
-
- Step 2: Find P and R parameters
- Let tube fluid be lower case (t), shell fluid be upper case (T).
- $P = (70 - 20) / (140 - 20) = 50 / 120 = 0.417$
- $R = (140 - 90) / (70 - 20) = 50 / 50 = 1.0$
-
- Step 3: From chart for 1-2 exchanger, at $P=0.417$, $R=1.0$, $F \approx 0.85$

Example 4: Final Area Calculation

- Step 4: Calculate Area
- Formula: $Q = U * A * F * \Delta T_{lm}$
- $150,000 \text{ W} = 400 \text{ W/m}^2\cdot\text{K} * A * 0.85 * 70 \text{ K}$
- $150,000 = A * (400 * 0.85 * 70)$
- $150,000 = A * 23,800$
- $\text{Area} = 150,000 / 23,800 = 6.30 \text{ m}^2$

Summary & Unit 4 Conclusion

- NTU Method is essential when outlet temperatures are unknown (rating/performance problems).
- Correction factor (F) is mandatory for multipass and cross-flow designs when using LMTD.
- This concludes Unit 4: Heat Exchangers. You should now be able to analyze and size various heat transfer equipment.