

Heat and Mass Transfer (DI05019071)

Complete Lecture Deck

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LMTD for Condensers and Evaporators

- Course: Heat and Mass Transfer (DI05019071)
- Unit 4: Heat Exchanger
- Lecture 33: Condensers, Evaporators, and Cross-flow

Lecture Agenda

- 1. Concept of Phase Change in Exchangers
- 2. Temperature Profiles in Condensers
- 3. Temperature Profiles in Evaporators
- 4. LMTD for Phase Change
- 5. Cross-flow and Multipass Exchangers
- 6. The Correction Factor (F)

Phase Change in Heat Exchangers

- In many industrial processes, one fluid undergoes a phase change (boiling or condensation).
- During phase change at a constant pressure, the temperature of the fluid remains constant.
- Specific heat capacity (c_p) is effectively infinite during phase change.
- Therefore, heat capacity rate ($C = m c_p$) approaches infinity.

Temperature Distribution in Condensers

- Hot fluid (vapor) condenses into liquid at a constant temperature (T_h).
- Cold fluid temperature (T_c) increases as it absorbs the latent heat.
- $T_{h,in} = T_{h,out} = T_h$ (constant line on the graph).
- T_c rises from $T_{c,in}$ to $T_{c,out}$.

Temperature Distribution in Evaporators

- Cold fluid (liquid) boils into vapor at a constant temperature (T_c).
- Hot fluid temperature (T_h) decreases as it provides the latent heat.
- $T_{c,in} = T_{c,out} = T_c$ (constant line on the graph).
- T_h drops from $T_{h,in}$ to $T_{h,out}$.

LMTD for Condensers and Evaporators

- Because one temperature is constant, ΔT_1 and ΔT_2 are the same regardless of flow direction.
- Parallel flow and counter flow arrangements give the exact same LMTD.
- Condenser: $\Delta T_1 = T_h - T_{c,in}$; $\Delta T_2 = T_h - T_{c,out}$
- Evaporator: $\Delta T_1 = T_{h,in} - T_c$; $\Delta T_2 = T_{h,out} - T_c$
- $LMTD = (\Delta T_1 - \Delta T_2) / \ln(\Delta T_1 / \Delta T_2)$

Beyond Parallel and Counter Flow

- Pure parallel or counter flow is often impractical for large surface areas.
- Industry uses Cross-flow (fluids flow perpendicular to each other).
- Industry also uses Multipass shell-and-tube exchangers (e.g., 1 shell pass, 2 tube passes).
- The standard LMTD formula assumes pure parallel or counter flow.

The Correction Factor (F)

- For cross-flow and multipass exchangers, we modify the LMTD equation.
- $q = U A F \text{ LMTD}_{cf}$
- Where LMTD_{cf} is the LMTD calculated assuming pure counter flow.
- F is a correction factor ($0 \leq F \leq 1$).
- If $F \leq 0.75$, the heat exchanger design is generally considered uneconomical.

How to Find F

- F is found using published charts (Bowman, Mueller, and Nagle charts).
- The charts depend on two dimensionless temperature ratios: P and R.
- P (Capacity ratio) = $(t_2 - t_1) / (T_1 - t_1)$
- R (Temperature ratio) = $(T_1 - T_2) / (t_2 - t_1)$
- (Where T = shell side temps, t = tube side temps)

Correction Factor for Phase Change

- What happens to the Correction Factor (F) in a condenser or evaporator?
- Since one fluid temperature is constant, $R = 0$ or $R = \text{infinity}$.
- Looking at the F -charts, for these values, $F = 1.0$ exactly.
- Conclusion: For phase change, $q = U A \text{ LMTD}$ (no correction needed for cross/multipass).

Steps for LMTD Method

- 1. Calculate heat duty (q) if temperatures and mass flows are known.
- 2. Determine unknown inlet/outlet temperatures using energy balance.
- 3. Calculate LMTD for counter flow arrangement.
- 4. Find P and R , then read F from the appropriate chart (if cross/multipass).
- 5. Calculate Area $A = q / (U F \text{ LMTD}_{cf})$.

Limitations of the LMTD Method

- LMTD is great for sizing problems (finding Area A when temps are known).
- LMTD is difficult for performance problems (finding outlet temps when A is known).
- If outlet temps are unknown, LMTD requires tedious trial-and-error iterations.
- To solve this, we will introduce the Effectiveness-NTU method in upcoming lectures.

Summary & Next Lecture

- Flow direction doesn't matter for condensers and evaporators.
- Cross-flow and multipass designs require a correction factor F .
- $F = 1$ for any phase change process.
- LMTD method requires iteration if outlet temperatures are unknown.
- Next Lecture: Overall Heat Transfer Coefficient and Fouling Factors.