

Question 1(a) [3 marks]

Define: 1) Branch 2) Junction 3) Mesh

Answer:

- **Branch:** A branch is a single circuit element or a combination of elements connected between two nodes of a network.
- **Junction:** A junction (or node) is a point in a circuit where two or more circuit elements are connected together.
- **Mesh:** A mesh is a closed path in a network where no other closed path exists inside it.

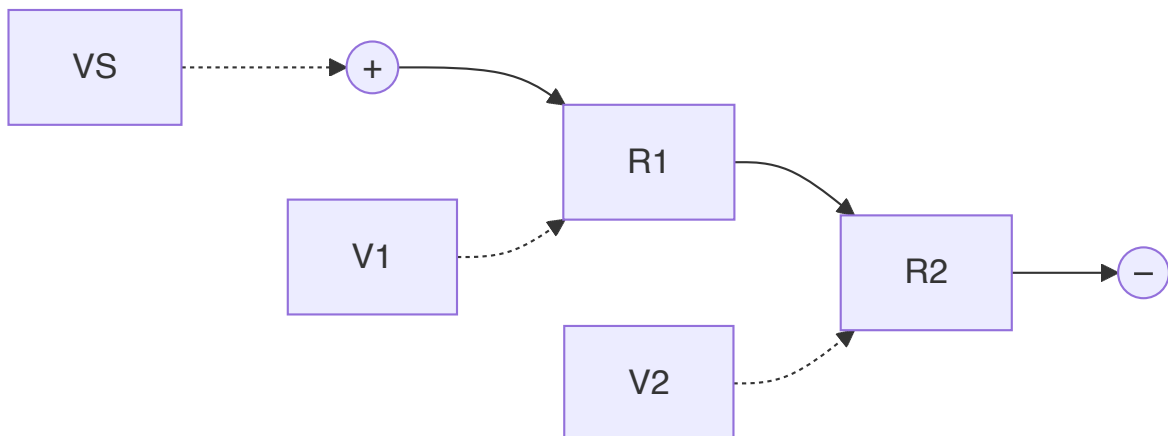
Mnemonic: "BJM: Branches Join at junctions to Make meshes"

Question 1(b) [4 marks]

Write voltage division and current division rule with necessary circuit diagram

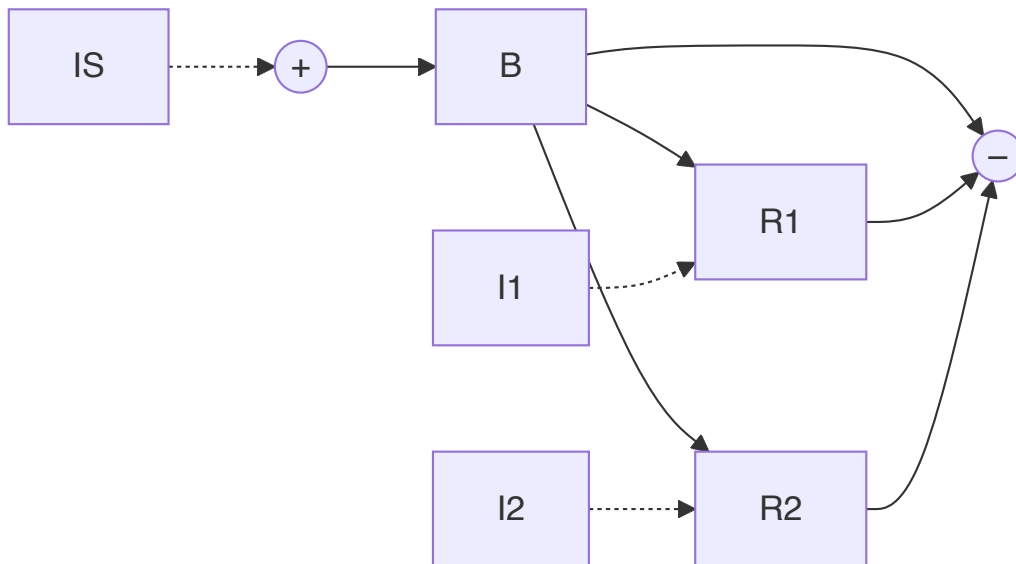
Answer:

Voltage Division Rule: In a series circuit, voltage across any component is proportional to its resistance.



- **Formula:** $V_1 = VS \times (R_1 / (R_1 + R_2))$
- **Application:** Used to find individual voltage drops across series components

Current Division Rule: In a parallel circuit, current through any branch is inversely proportional to its resistance.



- **Formula:** $I_1 = I_S \times (R_2 / (R_1 + R_2))$
- **Key concept:** Current takes path of least resistance

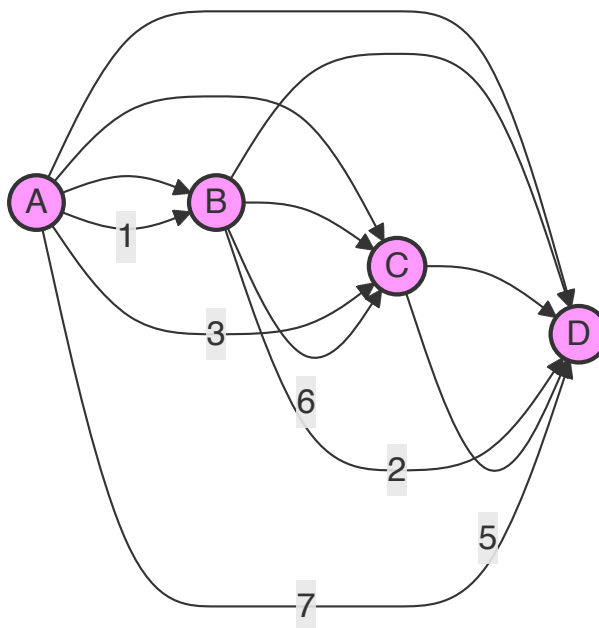
Mnemonic: "VoSe CuPa: Voltage divides in Series, Current divides in Parallel"

Question 1(c) [7 marks]

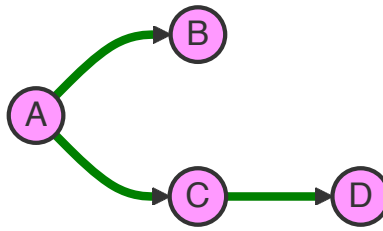
Draw Graph and Tree for a network shown in fig(1). Show link currents on a graph. Also write Tie-set schedule for a tree of network shown in fig. (1)

Answer:

Graph of the Network:



Tree of the Network (shown with bold edges):



Link Currents (shown on remaining branches that are not part of the tree):

- Link 1: Branch 2 (BD)
- Link 2: Branch 6 (BC)
- Link 3: Branch 7 (AD)
- Link 4: Branch 5 (CD)

Tie-set Schedule:

Link/Tree Branch	Branch 1 (AB)	Branch 3 (AC)	Branch 4 (CD)	Branch 2 (BD)	Branch 6 (BC)	Branch 7 (AD)	Branch 5 (CD)
Link 1 (BD)	1	0	0	1	0	0	0
Link 2 (BC)	1	1	0	0	1	0	0
Link 3 (AD)	0	0	1	0	0	1	0
Link 4 (CD)	0	0	1	0	0	0	1

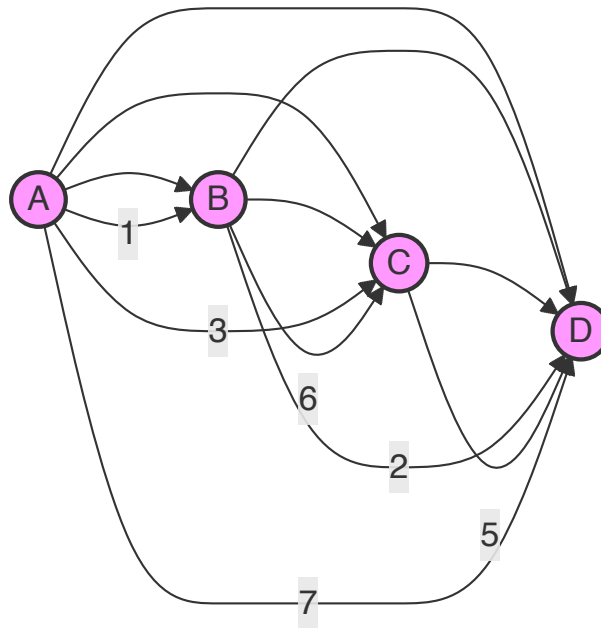
Mnemonic: "TGLT: Trees Generate Link-current Tie-sets"

Question 1(c) OR [7 marks]

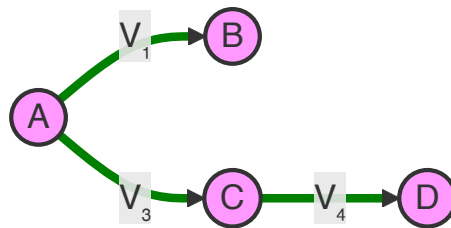
Draw Graph and Tree for a network shown in fig(1). Show branch voltages on tree. Also write cut-set schedule for a tree of network shown on fig.(1)

Answer:

Graph of the Network:



Tree of the Network (shown with bold edges and branch voltages):



Cut-set Schedule:

Cut-set/Branch	Branch 1 (AB)	Branch 3 (AC)	Branch 4 (CD)	Branch 2 (BD)	Branch 6 (BC)	Branch 7 (AD)	Branch 5 (CD)
Cut-set 1 (AB)	1	0	0	-1	-1	0	0
Cut-set 2 (AC)	0	1	0	0	1	-1	0
Cut-set 3 (CD)	0	0	1	1	0	1	1

Mnemonic: "CGVS: Cut-sets Generate Voltage Sources"

Question 2(a) [3 marks]

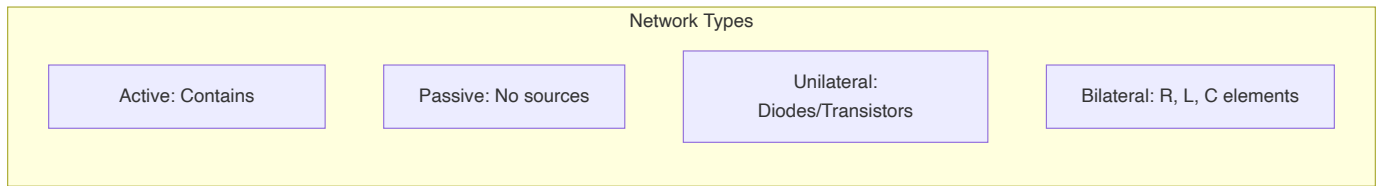
Define: 1) Active and passive network 2) Unilateral and Bilateral network.

Answer:

- **Active Network:** A network containing one or more sources of EMF (voltage/current sources) that supply energy to the circuit.
- **Passive Network:** A network containing only passive elements like resistors, capacitors, and inductors with no energy sources.
- **Unilateral Network:** A network in which the properties and performance change when input and output terminals are interchanged.

- **Bilateral Network:** A network in which the properties and performance remain unchanged when input and output terminals are interchanged.

Diagram:



Mnemonic: "APUB: Active Provides energy, Unilateral Blocks reversal"

Question 2(b) [4 marks]

Write equation for Z parameter and derive Z11, Z12, Z21, Z22 from that equation.

Answer:

Z-parameters define the relationship between port voltages and currents in a two-port network:

Equations:

- $V_1 = Z_{11}I_1 + Z_{12}I_2$
- $V_2 = Z_{21}I_1 + Z_{22}I_2$

Derivation:

- $Z_{11} = V_1/I_1$ (with $I_2 = 0$): Input impedance with output port open-circuited
- $Z_{12} = V_1/I_2$ (with $I_1 = 0$): Reverse transfer impedance with input port open-circuited
- $Z_{21} = V_2/I_1$ (with $I_2 = 0$): Forward transfer impedance with output port open-circuited
- $Z_{22} = V_2/I_2$ (with $I_1 = 0$): Output impedance with input port open-circuited

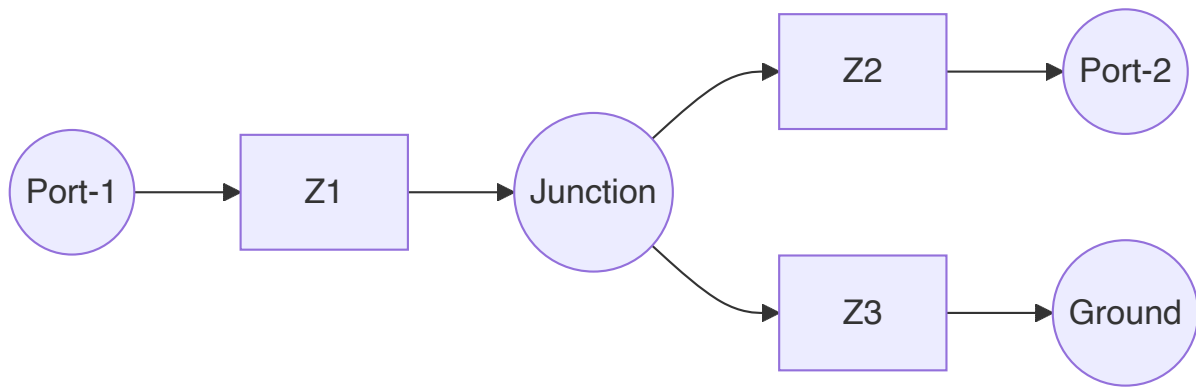
Mnemonic: "Z Impedance: Open circuit gives correct Parameters"

Question 2(c) [7 marks]

Derive equation of characteristic impedance(ZOT) for a standard T network.

Answer:

For a standard T-network:

**Derivation Steps:**

1. For a symmetric T-network, $Z_1 = Z_2$
2. Under matched condition, input impedance equals characteristic impedance
3. $Z_{ot} = Z_1 + (Z_1 \times Z_3) / (Z_1 + Z_3)$
4. For balanced T-network where $Z_1 = Z_2 = Z/2$ and $Z_3 = Z$:
5. $Z_{ot} = Z/2 + (Z/2 \times Z) / (Z/2 + Z)$
6. $Z_{ot} = Z/2 + (Z^2/2) / (Z + Z/2)$
7. $Z_{ot} = Z/2 + (Z^2/2) / (3Z/2)$
8. $Z_{ot} = Z/2 + Z^2/3Z$
9. $Z_{ot} = Z/2 + Z/3$
10. $Z_{ot} = (3Z + 2Z)/6$
11. $Z_{ot} = \sqrt{Z_1(Z_1 + 2Z_3)}$

Final Equation: $Z_{ot} = \sqrt{Z_1(Z_1 + 2Z_3)}$

Mnemonic: "TO Impedance: Two arms Over middle branch"

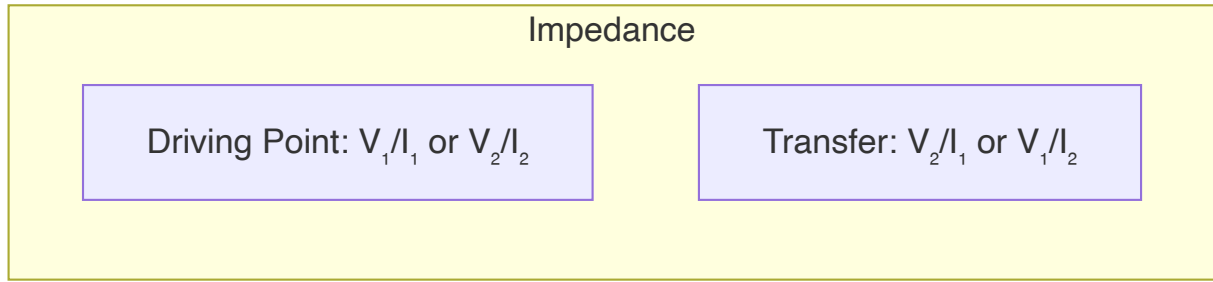
Question 2(a) OR [3 marks]

Define: 1) Driving point impedance 2) Transfer impedance

Answer:

- **Driving Point Impedance:** The ratio of voltage to current at the same port/pair of terminals when all other independent sources are set to zero.
- **Transfer Impedance:** The ratio of voltage at one port to the current at another port when all other independent sources are set to zero.

Diagram:



Mnemonic: "DTSS: Driving at Terminal Same, Transfer at Separate"

Question 2(b) OR [4 marks]

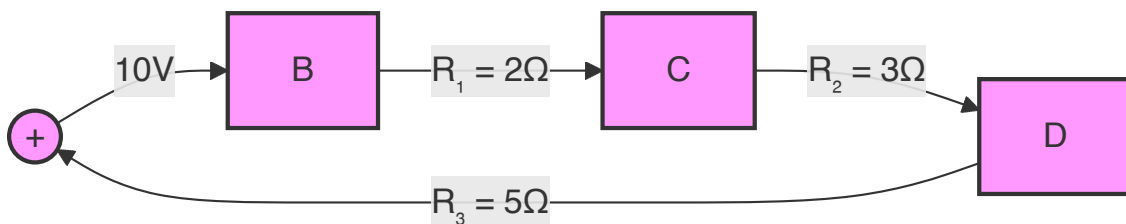
Explain Kirchhoff's voltage law with example.

Answer:

Kirchhoff's Voltage Law (KVL): The algebraic sum of all voltages around any closed loop in a circuit is zero.

Mathematically: $\sum V = 0$ (around a closed loop)

Circuit Example:



If $I = 1A$, then:

- $V_1 = 1A \times 2\Omega = 2V$
- $V_2 = 1A \times 3\Omega = 3V$
- $V_3 = 1A \times 5\Omega = 5V$

Applying KVL: $10V - 2V - 3V - 5V = 0 \checkmark$

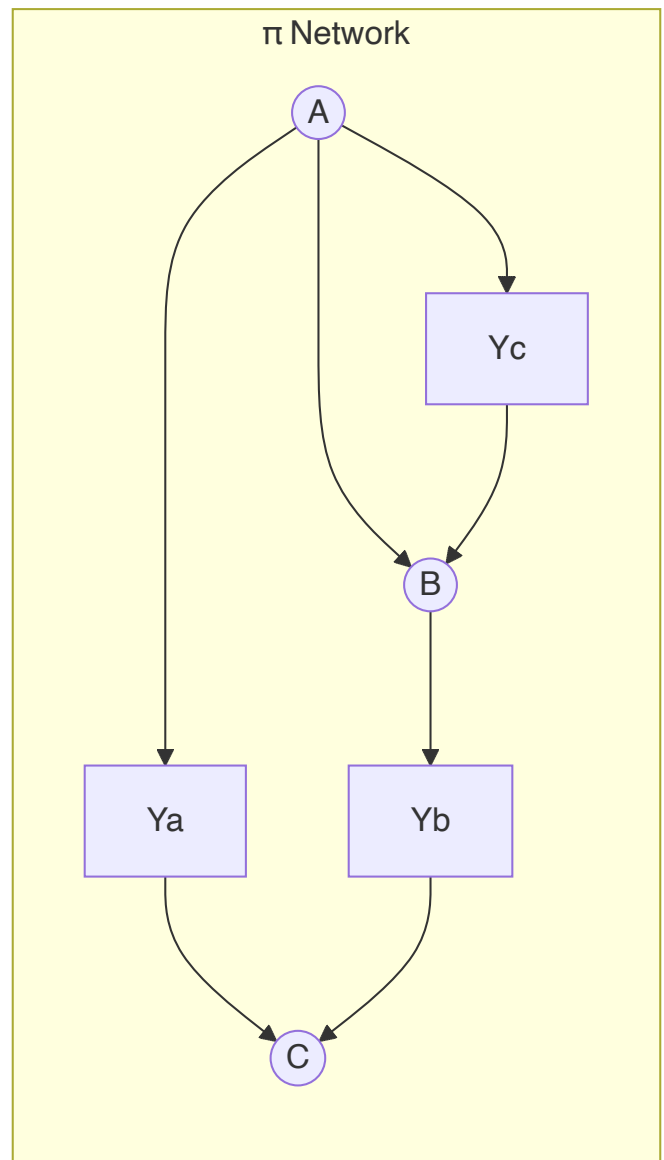
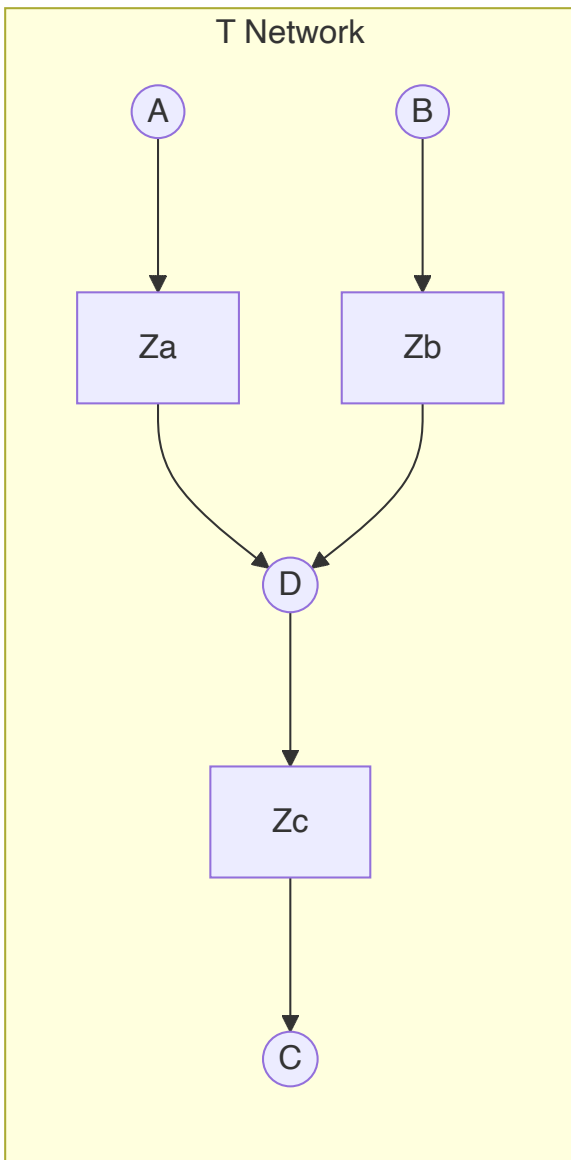
Mnemonic: "VACZ: Voltages Around Closed loop are Zero"

Question 2(c) OR [7 marks]

Derive equation to convert π network into T network.

Answer:

π Network to T Network Conversion:

**Conversion Equations:**

1. $Z_a = (Y_a \times Y_c) / Y_{\Delta}$
2. $Z_b = (Y_b \times Y_c) / Y_{\Delta}$
3. $Z_c = (Y_a \times Y_b) / Y_{\Delta}$

Where $Y_{\Delta} = Y_a + Y_b + Y_c$

Derivation:

1. Start with Y-parameters of π -network
2. Express Y-parameters in terms of branch admittances
3. Convert to Z-parameters using matrix inversion
4. Express T-network impedances in terms of Z-parameters
5. Simplify to get the conversion formulas above

Mnemonic: "PIE to TEA: Product over sum for opposite branch"

Question 3(a) [3 marks]

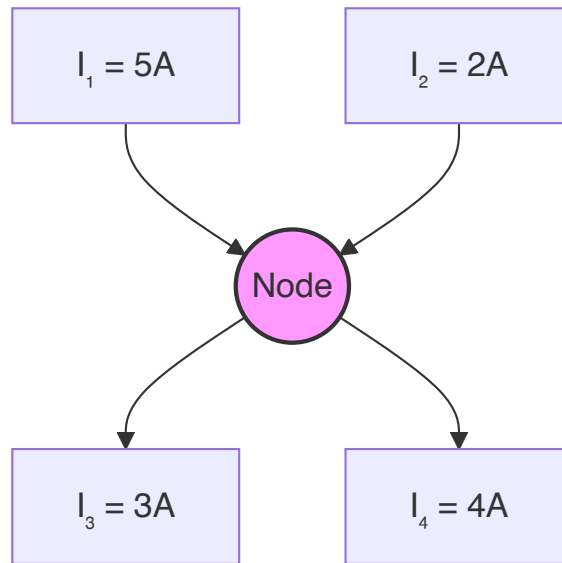
Explain Kirchhoff's current law with example.

Answer:

Kirchhoff's Current Law (KCL): The algebraic sum of all currents entering and leaving a node must equal zero.

Mathematically: $\sum I = 0$ (at any node)

Circuit Example:



Applying KCL at node B:

- Currents entering: $I_1 + I_2 = 5A + 2A = 7A$
- Currents leaving: $I_3 + I_4 = 3A + 4A = 7A$
- Therefore: $I_1 + I_2 - I_3 - I_4 = 5 + 2 - 3 - 4 = 0 \checkmark$

Mnemonic: "CuNoZ: Currents at Node are Zero"

Question 3(b) [4 marks]

Explain mesh analysis with required equations.

Answer:

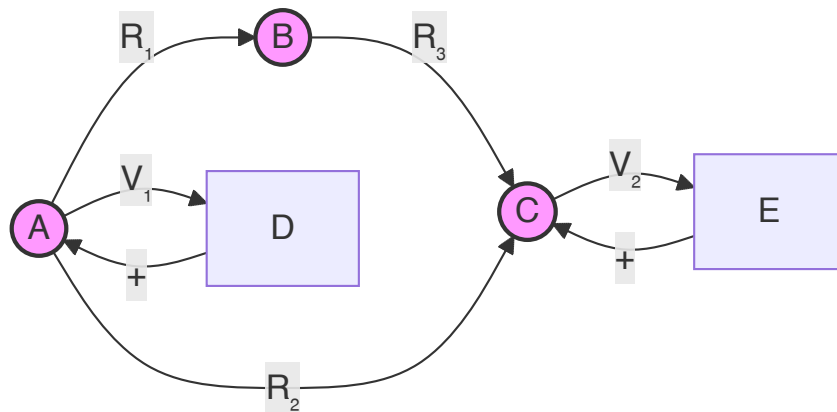
Mesh Analysis: A circuit analysis technique that uses mesh currents as variables to solve a circuit with multiple loops.

Steps:

1. Identify all meshes (closed loops) in the circuit
2. Assign a mesh current to each mesh
3. Apply KVL to each mesh

4. Solve the resulting system of equations

Example Circuit:



Equations:

- Mesh 1: $V_1 = I_1 R_1 + I_1 R_2 - I_2 R_2$
- Mesh 2: $V_2 = I_2 R_2 + I_2 R_3 - I_1 R_2$

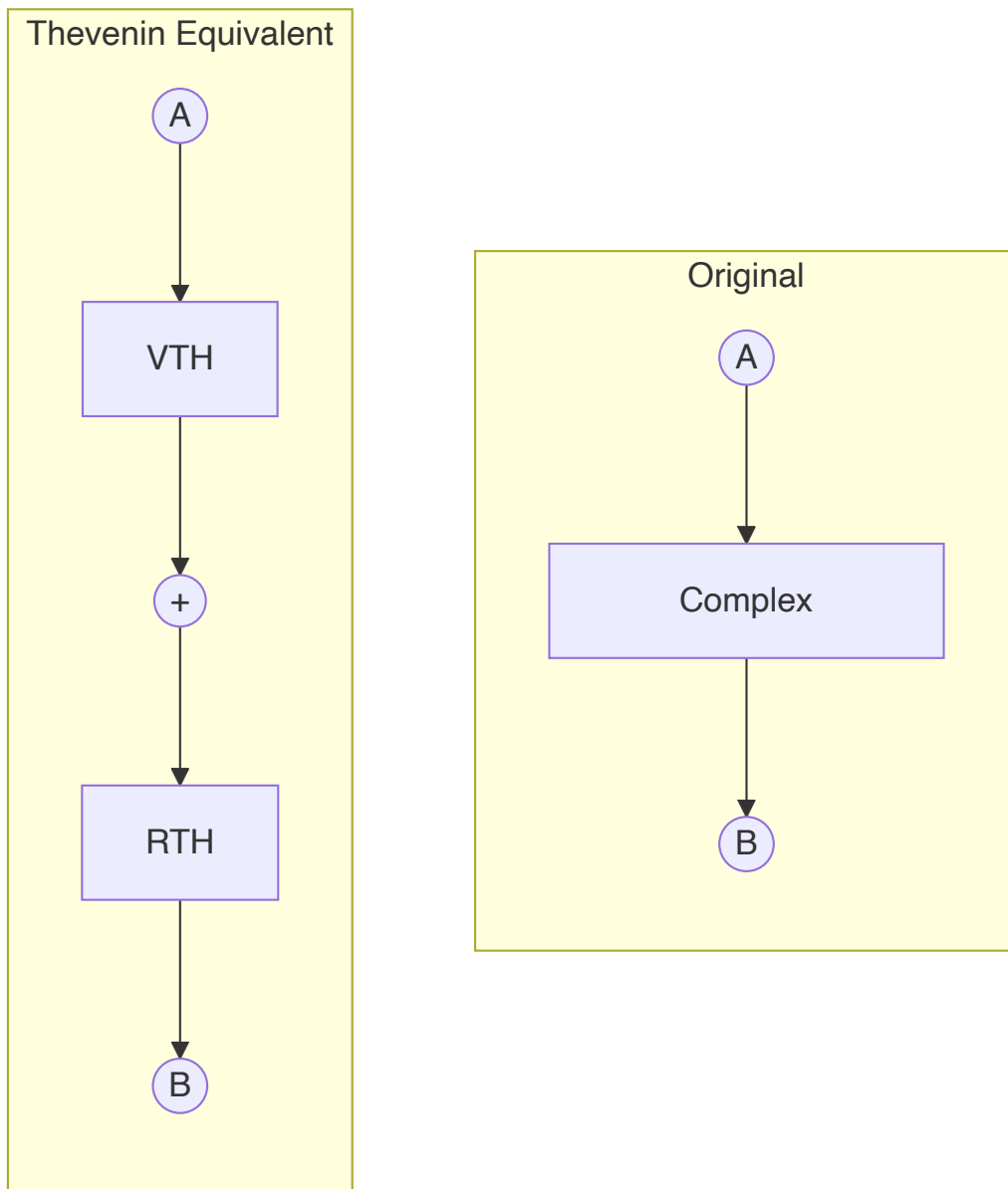
Mnemonic: "MILK: Mesh Is Loop with KVL"

Question 3(c) [7 marks]

State and explain Thevenin's theorem.

Answer:

Thevenin's Theorem: Any linear network with voltage and current sources can be replaced by an equivalent circuit consisting of a voltage source (V_{TH}) in series with a resistance (R_{TH}).



Steps to Find Thevenin Equivalent:

1. Remove the load from the terminals of interest
2. Calculate the open-circuit voltage (VOC) across these terminals (= VTH)
3. Calculate the resistance looking back into the circuit with all sources replaced by their internal resistances (= RTH)
4. The Thevenin equivalent consists of VTH in series with RTH

Example Application:

- Original complex circuit with load RL
- Remove RL and find VOC = VTH
- Deactivate sources and find RTH
- Reconnect RL to simplified Thevenin equivalent

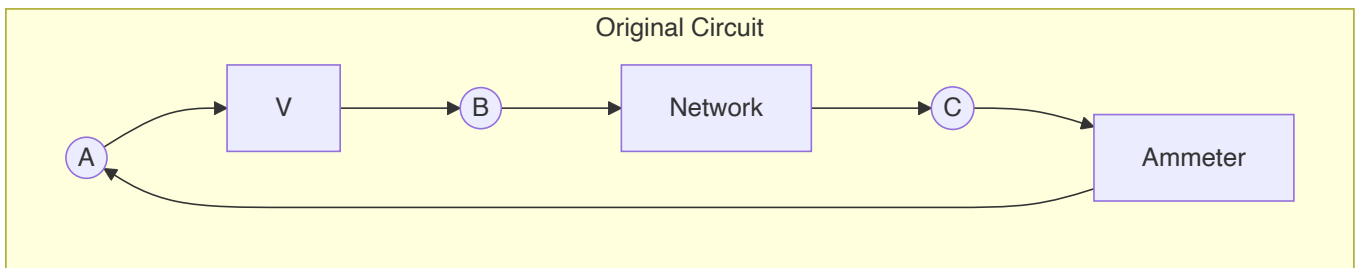
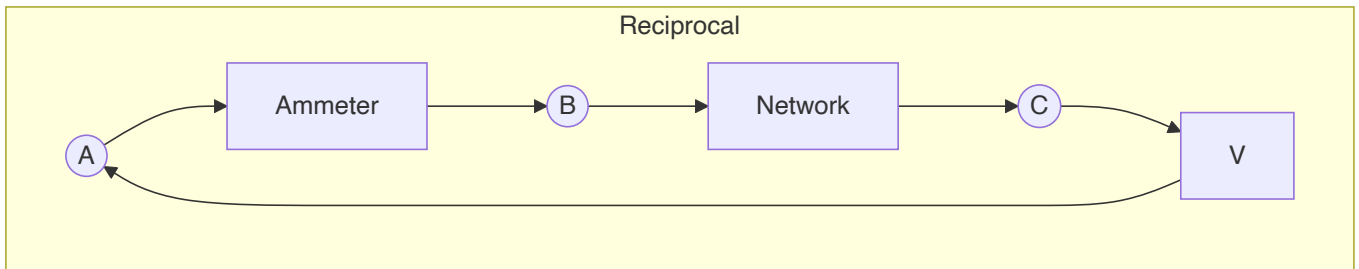
Mnemonic: "TORV: Thevenin's Open-circuit Resistance and Voltage"

Question 3(a) OR [3 marks]

State and explain reciprocity theorem.

Answer:

Reciprocity Theorem: In a linear, bilateral network, if a voltage source in one branch produces a current in another branch, then the same voltage source, if placed in the second branch, will produce the same current in the first branch.



Mathematically: If a voltage V_1 in branch 1 produces current I_2 in branch 2, then voltage V_1 in branch 2 will produce current I_2 in branch 1.

Limitations: Applies only to networks with:

- Linear elements
- Bilateral elements (no diodes, transistors)
- Single independent source

Mnemonic: "RESWAP: REciprocity SWAPs Position with identical results"

Question 3(b) OR [4 marks]

Explain nodal analysis with required equations.

Answer:

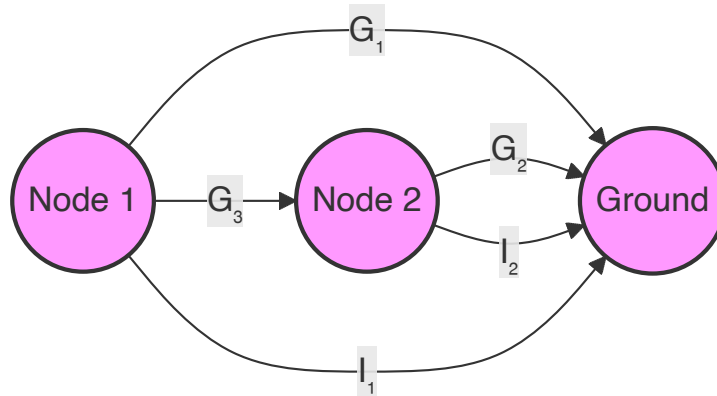
Nodal Analysis: A circuit analysis technique that uses node voltages as variables to solve a circuit.

Steps:

1. Choose a reference node (ground)
2. Assign voltage variables to remaining nodes

3. Apply KCL at each non-reference node
4. Solve the resulting system of equations

Example Circuit:



Equations:

- Node 1: $I_1 = V_1 G_1 + (V_1 - V_2) G_3$
- Node 2: $I_2 = V_2 G_2 + (V_2 - V_1) G_3$

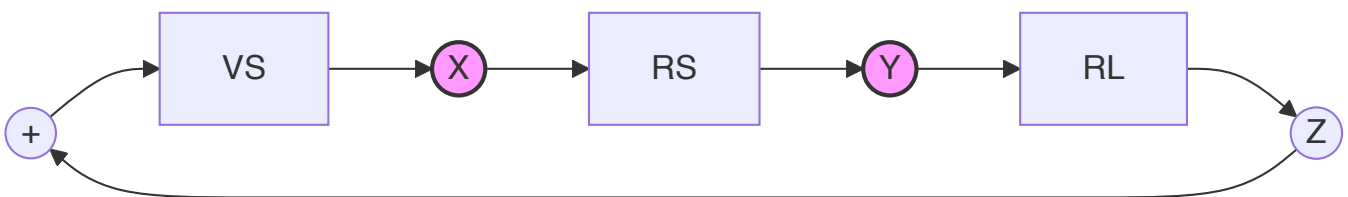
Mnemonic: "NKCV: Nodal uses KCL with Voltage variables"

Question 3(c) OR [7 marks]

State and prove maximum power transfer theorem.

Answer:

Maximum Power Transfer Theorem: A load connected to a source will extract maximum power when its resistance equals the internal resistance of the source.



Proof:

1. Current in the circuit: $I = V_S / (R_S + R_L)$
2. Power delivered to load: $P = I^2 R_L = (V_S^2 R_L) / (R_S + R_L)^2$
3. For maximum power, $dP/dR_L = 0$
4. Solving: $(V_S^2 (R_S + R_L)^2 - V_S^2 R_L \cdot 2(R_S + R_L)) / (R_S + R_L)^4 = 0$
5. Simplifying: $(R_S + R_L)^2 = 2R_L (R_S + R_L)$
6. Further simplifying: $R_S + R_L = 2R_L$
7. Therefore: $R_S = R_L$

Maximum Power: $P_{max} = V_S^2 / (4R_S)$

Mnemonic: "MaRLRS: Maximum power when load Resistance equals Source Resistance"

Question 4(a) [3 marks]

Why series resonance circuit act as voltage amplifier and parallel resonance circuit act as current amplifier?

Answer:

Series Resonance as Voltage Amplifier:

- At resonance, series circuit impedance is minimum (just R)
- Voltage across L or C can be much larger than source voltage
- Voltage magnification factor = $Q = X_L / R = 1 / R \sqrt{L / C}$
- Voltage across L or C = $Q \times$ Source voltage

Parallel Resonance as Current Amplifier:

- At resonance, parallel circuit impedance is maximum
- Current in L or C can be much larger than source current
- Current magnification factor = $Q = R / X_L = R \sqrt{C / L}$
- Current through L or C = $Q \times$ Source current

Table:

Circuit Type	Impedance at Resonance	Amplification
Series	Minimum (R only)	Voltage (V_L or $V_C = Q \times V_S$)
Parallel	Maximum (R^2 / r)	Current (I_L or $I_C = Q \times I_S$)

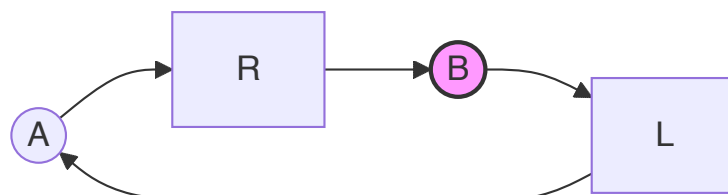
Mnemonic: "SeVoPa: Series Voltage, Parallel current amplification"

Question 4(b) [4 marks]

Derive equation of Q of coil.

Answer:

Q-factor of a Coil:



Derivation:

1. Q-factor is defined as: $Q = \text{Energy stored} / \text{Energy dissipated per cycle}$
2. Energy stored in inductor = $(1/2)LI^2$
3. Power dissipated in resistor = I^2R
4. Energy dissipated per cycle = Power \times Time period = $I^2R \times (1/f)$
5. Therefore: $Q = ((1/2)LI^2) / (I^2R \times (1/f))$
6. Simplifying: $Q = 2\pi \times (1/2)LI^2 \times f / (I^2R)$
7. $Q = 2\pi f \times L / R = \omega L / R$

Final Equation: $Q = \omega L / R = 2\pi fL / R = X_L / R$

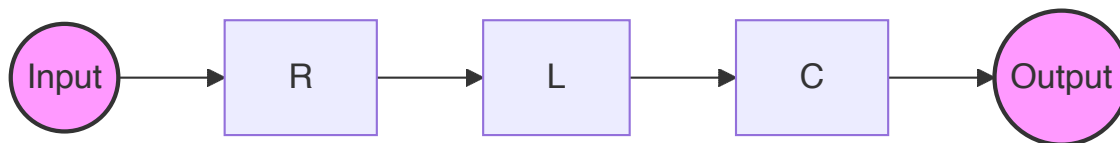
Mnemonic: "QualityEDR: Quality equals Energy stored Divided by energy lost per Radian"

Question 4(c) [7 marks]

Derive equation of series resonance frequency for series R-L-C circuit.

Answer:

Series R-L-C Circuit:

**Derivation:**

1. Impedance of series RLC circuit: $Z = R + j(X_L - X_C)$
2. Where: $X_L = \omega L$ and $X_C = 1/\omega C$
3. At resonance, $X_L = X_C$ (inductive and capacitive reactances are equal)
4. Therefore: $\omega L = 1/\omega C$
5. Solving for ω : $\omega^2 = 1/LC$
6. Resonant frequency: $\omega_0 = 1/\sqrt{LC}$
7. In terms of frequency f : $f_0 = 1/(2\pi\sqrt{LC})$

Characteristics at Resonance:

- Impedance is minimum (purely resistive: $Z = R$)
- Current is maximum ($I = V/R$)
- Power factor is unity (circuit appears resistive)
- Voltages across L and C are equal and opposite

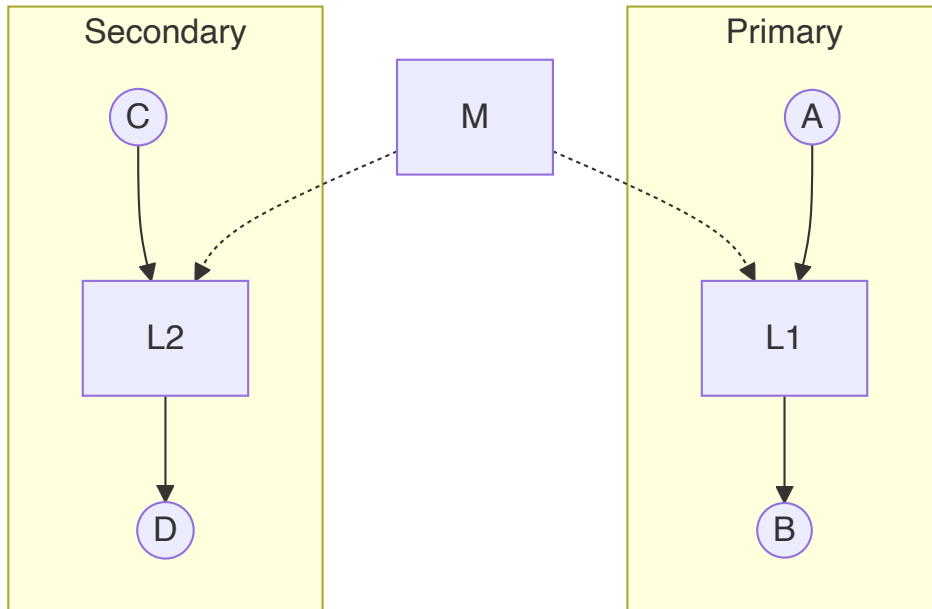
Mnemonic: "RES: Reactances Equal at Series resonance"

Question 4(a) OR [3 marks]

What is coupled circuits? Define self-inductance and mutual inductance.

Answer:

Coupled Circuits: Two or more circuits that are magnetically linked such that energy can be transferred between them through their mutual magnetic field.



Self-inductance (L): The property of a circuit whereby a change in current produces a self-induced EMF in the same circuit.

$$L = \Phi / I \text{ (ratio of magnetic flux to the current producing it)}$$

Mutual inductance (M): The property of a circuit whereby a change in current in one circuit induces an EMF in another circuit.

$$M = \Phi_{21} / I_1 \text{ (ratio of flux in circuit 2 due to current in circuit 1)}$$

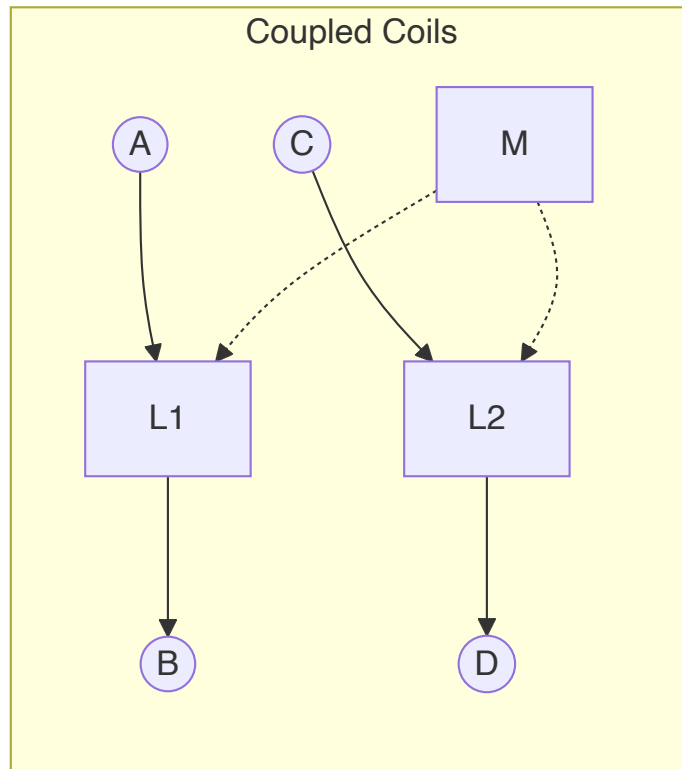
Mnemonic: "SiMu: Self in Mine, Mutual in Yours"

Question 4(b) OR [4 marks]

Derive equation for co-efficient of coupling (K).

Answer:

Coefficient of Coupling (k):

**Derivation:**

1. The mutual inductance (M) between two coils depends on:
 - Self-inductances of the coils (L_1 and L_2)
 - Physical arrangement (proximity and orientation)
2. Maximum possible mutual inductance: $M_{m_{ax}} = \sqrt{L_1 L_2}$
3. Coefficient of coupling is defined as: $k = M/M_{m_{ax}}$
4. Therefore: $k = M/\sqrt{L_1 L_2}$

Characteristics:

- k ranges from 0 (no coupling) to 1 (perfect coupling)
- k depends on geometry, orientation, and medium
- Typical transformers: $k = 0.95$ to 0.99
- Air-core coils: $k = 0.01$ to 0.5

Mnemonic: "KMutual: K Measures Mutual linkage proportion"

Question 4(c) OR [7 marks]

A series RLC circuit has $R=30\Omega$, $L=0.5H$, and $C=5\mu F$. Calculate (i) series resonance frequency (2) Q Factor (3)BW

Answer:

Given:

- Resistance, $R = 30\Omega$
- Inductance, $L = 0.5\text{H}$
- Capacitance, $C = 5\mu\text{F} = 5 \times 10^{-6}\text{F}$

Calculations:**(i) Series Resonance Frequency:**

- $f_0 = 1/(2\pi\sqrt{LC})$
- $f_0 = 1/(2\pi\sqrt{(0.5 \times 5 \times 10^{-6})})$
- $f_0 = 1/(2\pi\sqrt{(2.5 \times 10^{-6})})$
- $f_0 = 1/(2\pi \times 1.58 \times 10^{-3})$
- $f_0 = 1/(9.9 \times 10^{-3})$
- $f_0 = 100.76 \text{ Hz}$
- $f_0 \approx 100 \text{ Hz}$

(ii) Q Factor:

- $Q = (1/R)\sqrt{L/C}$
- $Q = (1/30)\sqrt{(0.5/(5 \times 10^{-6}))}$
- $Q = (1/30)\sqrt{(100,000)}$
- $Q = (1/30) \times 316.23$
- $Q = 10.54$

(iii) Bandwidth (BW):

- $\text{BW} = f_0/Q$
- $\text{BW} = 100.76/10.54$
- $\text{BW} = 9.56 \text{ Hz}$

Table:

Parameter	Formula	Value
Resonant Frequency (f_0)	$1/(2\pi\sqrt{LC})$	100 Hz
Quality Factor (Q)	$(1/R)\sqrt{L/C}$	10.54
Bandwidth (BW)	f_0/Q	9.56 Hz

Mnemonic: "RQB: Resonance Quality determines Bandwidth"

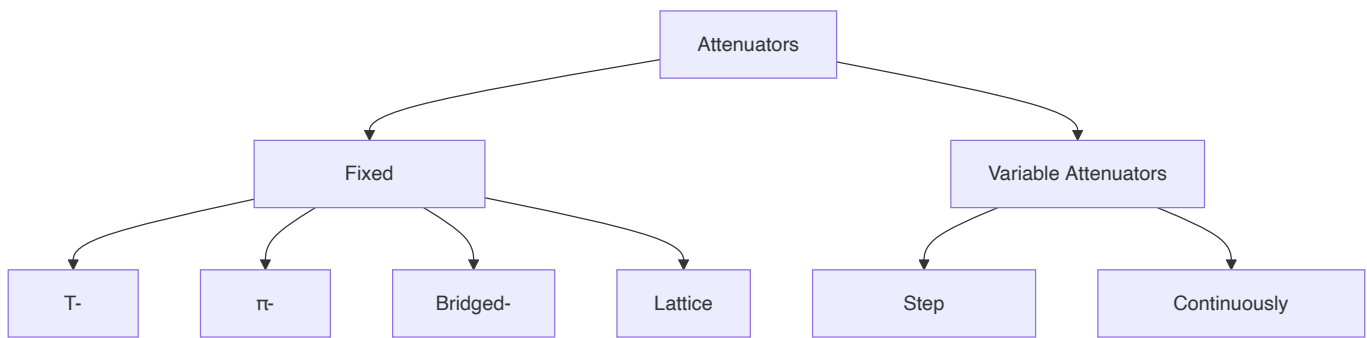
Question 5(a) [3 marks]

Classify various types of attenuators.

Answer:

Attenuators: Network of resistors designed to reduce (attenuate) signal level without distortion.

Types of Attenuators:



Based on configuration:

- **T-type:** Three resistor T-shaped configuration
- **π-type:** Three resistor π-shaped configuration
- **Bridged-T:** T-type with a resistor bridging across
- **Lattice:** Balanced configuration with four resistors

Based on symmetry:

- **Symmetrical:** Equal input and output impedance
- **Asymmetrical:** Different input and output impedance

Mnemonic: "ATP Fixed: Attenuator Types include Pad, Tee, Lattice"

Question 5(b) [4 marks]

Derive relation between attenuator and neper.

Answer:

Relationship between Attenuation and Neper:

- **Attenuation (α):** Ratio of input voltage (or current) to output voltage (or current), expressed in different units.
- **Neper (Np):** Natural logarithmic unit of ratios, used mainly in transmission line theory.

Derivation:

1. For a voltage ratio V_1/V_2 :
 - Attenuation in Nepers = $\ln(V_1/V_2)$
 - Attenuation in Decibels = $20\log_{10}(V_1/V_2)$
2. For a power ratio P_1/P_2 :
 - Attenuation in Nepers = $(1/2)\ln(P_1/P_2)$
 - Attenuation in Decibels = $10\log_{10}(P_1/P_2)$
3. Relationship between dB and Neper:

- 1 Neper = 8.686 dB
- 1 dB = 0.115 Neper

Table:

Unit	Voltage Ratio	Power Ratio
Neper (Np)	$\ln(V_1/V_2)$	$(1/2)\ln(P_1/P_2)$
Decibel (dB)	$20\log_{10}(V_1/V_2)$	$10\log_{10}(P_1/P_2)$

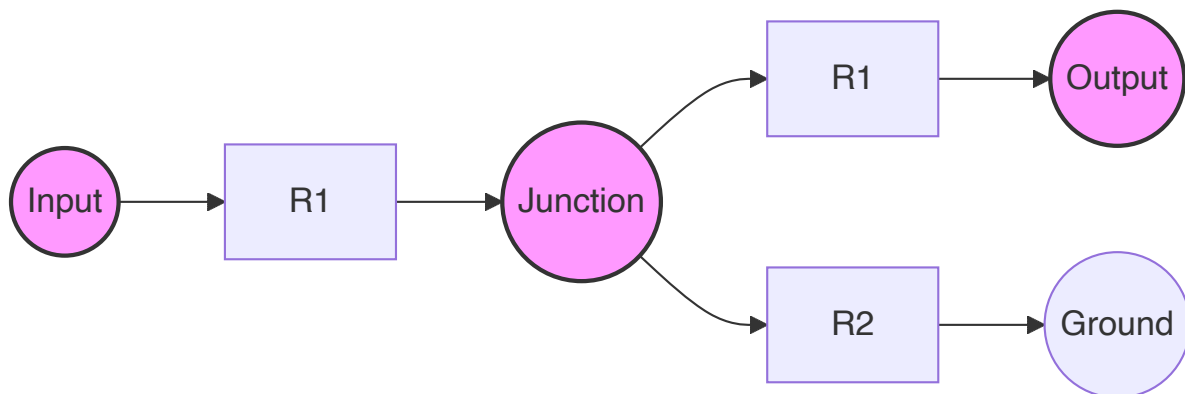
Mnemonic: "NED: Neper Equals Decibel divided by 8.686"

Question 5(c) [7 marks]

Derive equations of R1 and R2 for symmetrical T attenuator.

Answer:

Symmetrical T Attenuator:



Derivation:

- For a symmetrical T-attenuator with characteristic impedance Z_0 :
 - Input and output impedance must both equal Z_0
 - Attenuation ratio $N = V_1/V_2 = I_2/I_1$
- From circuit analysis:
 - $Z_0 = R_1 + (R_2(R_1))/(R_2+R_1)$
 - $N = (R_1 + R_2 + R_1)/R_2 = (2R_1+R_2)/R_2$
- Solving for R_1 and R_2 :
 - $R_1 = Z_0(N-1)/(N+1)$
 - $R_2 = 2Z_0N/(N^2-1)$
- For attenuation in dB (α):
 - $N = 10^{(\alpha/20)}$

- o $R_1 = Z_0 \cdot \tanh(\alpha/2)$
- o $R_2 = Z_0 / \sinh(\alpha)$

Final Equations:

- $R_1 = Z_0(N-1)/(N+1)$
- $R_2 = 2Z_0N/(N^2-1)$

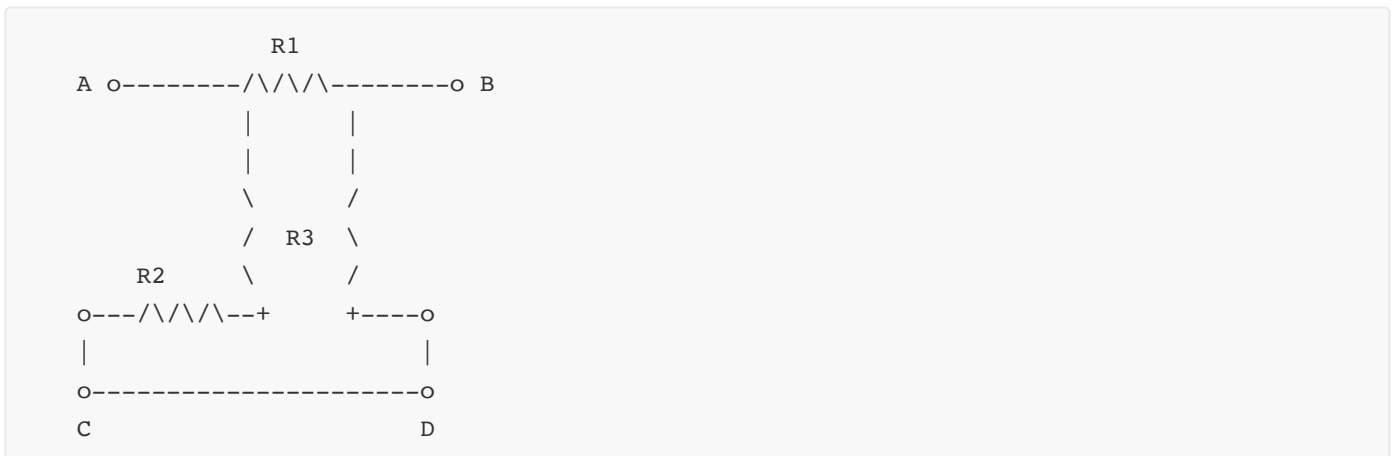
Mnemonic: "TSR: T-attenuator Symmetry Requires equal R1 values"

Question 5(a) OR [3 marks]

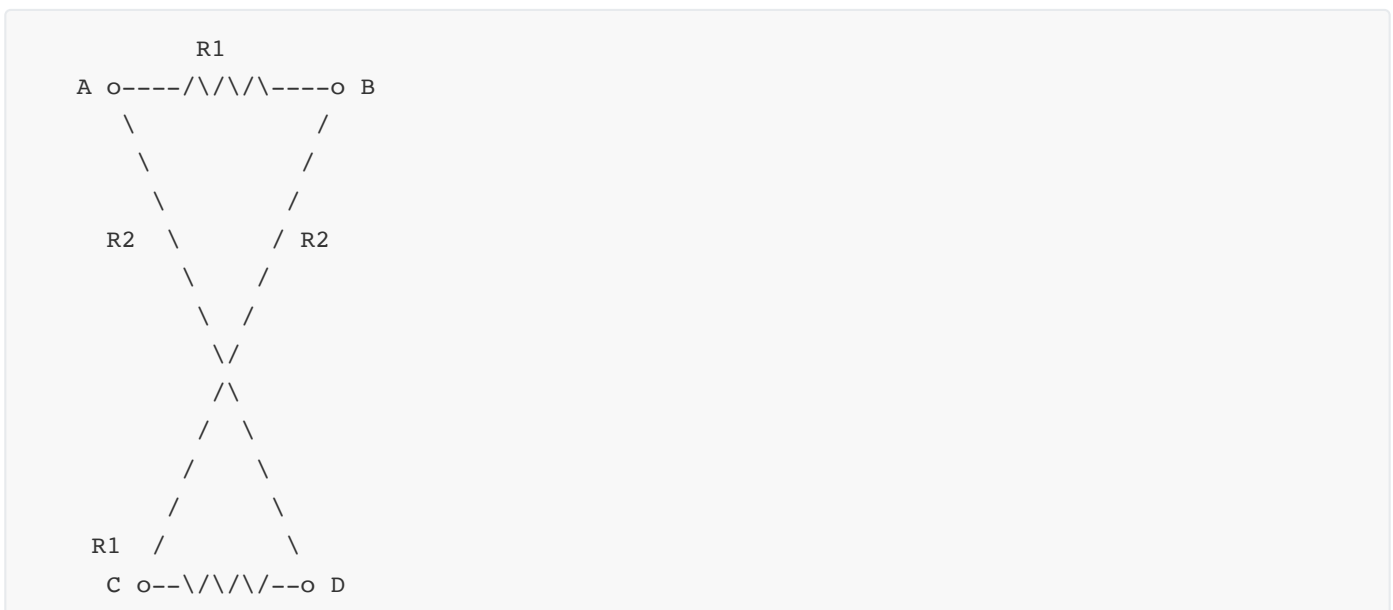
Draw circuit diagram of symmetrical Bridge T and symmetrical Lattice attenuator.

Answer:

Symmetrical Bridge-T Attenuator:



Symmetrical Lattice Attenuator:



Characteristics:

1. **Bridge-T:** Combines features of T and π attenuators, suitable for high-frequency applications

2. **Lattice:** Balanced configuration with excellent phase and frequency response, commonly used in balanced lines

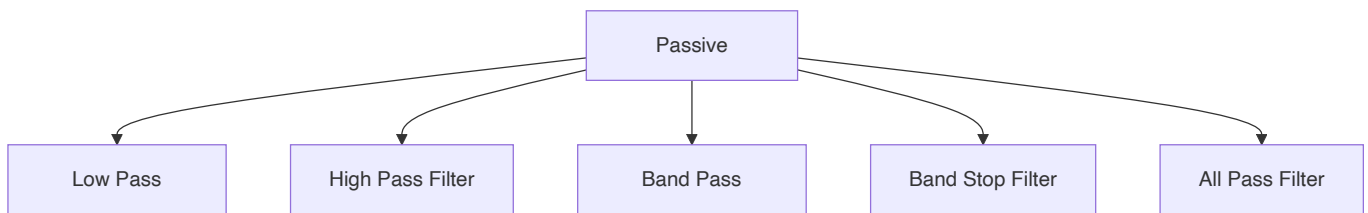
Mnemonic: "BL-BA: Bridge Ladder, Balanced Attenuators"

Question 5(b) OR [4 marks]

Write classification of filter based on frequency with their frequency responses showing pass band and stop band.

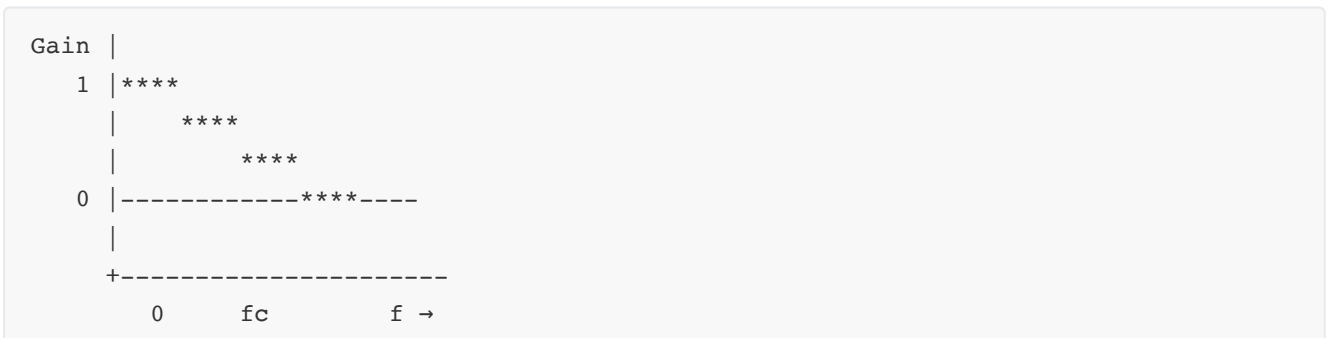
Answer:

Classification of Filters Based on Frequency:

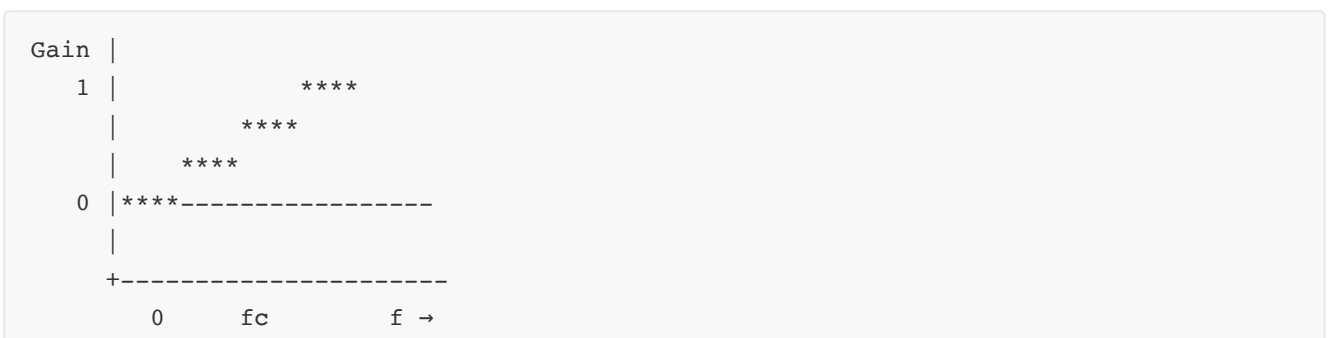


Frequency Responses:

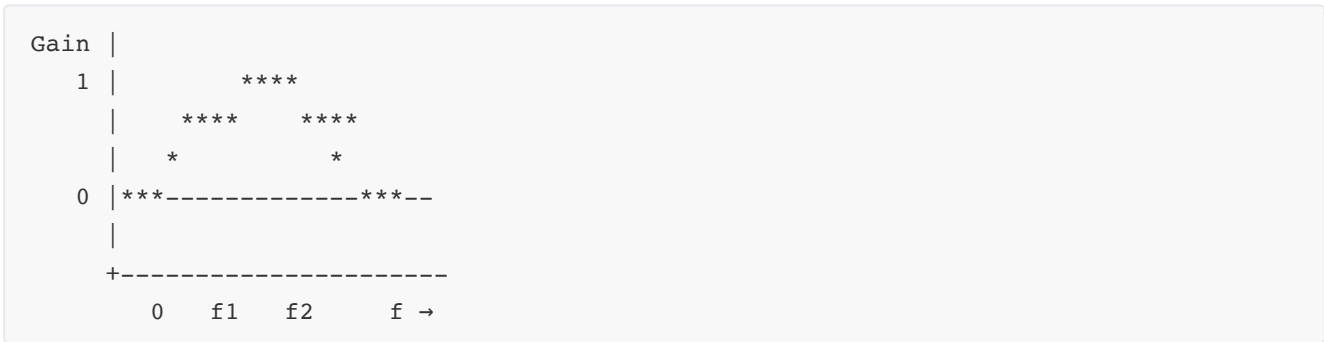
1. **Low Pass Filter:** Passes frequencies below cutoff, attenuates above



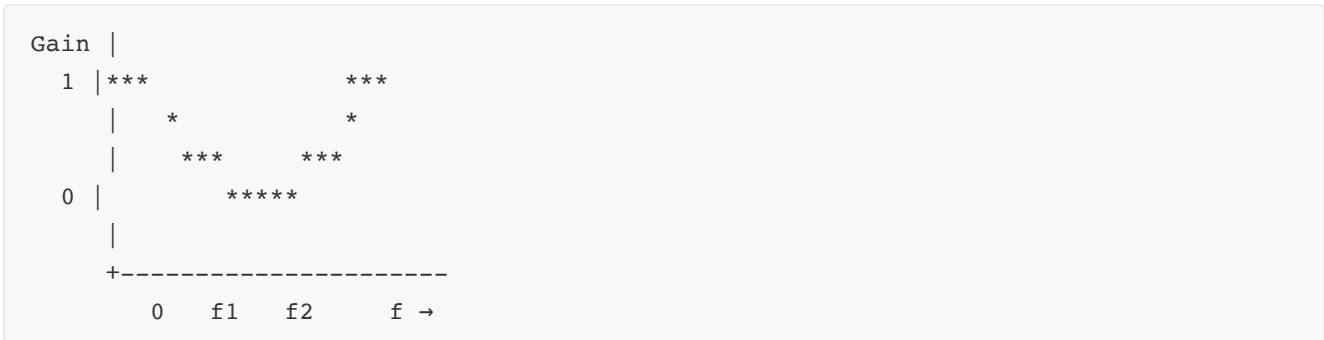
2. **High Pass Filter:** Passes frequencies above cutoff, attenuates below



3. **Band Pass Filter:** Passes frequencies within a specific band



4. **Band Stop Filter:** Rejects frequencies within a specific band



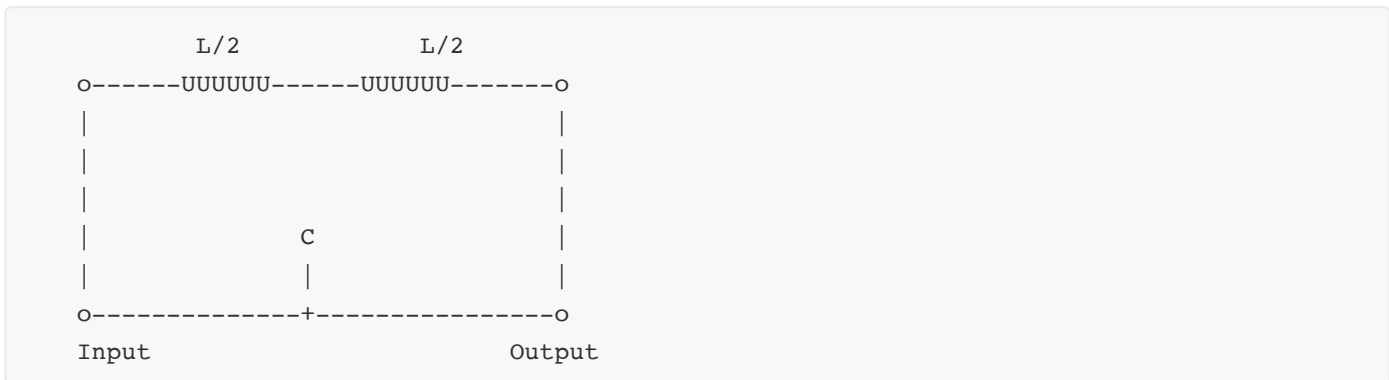
Mnemonic: "LHBBBA: Low High Band-pass Band-stop All-pass"

Question 5(c) OR [7 marks]

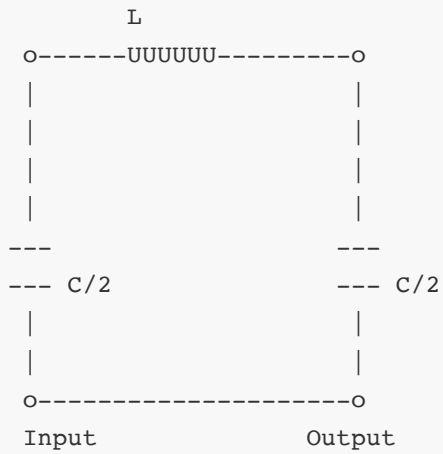
Draw the circuit for T-section and π -section constant-K low pass filter and Derive equation of cut-off frequency.

Answer:

T-section Constant-K Low Pass Filter:



π -section Constant-K Low Pass Filter:



Derivation of Cutoff Frequency:

1. For a constant-K filter:
 - $Z_1 \times Z_2 = R_0^2$ (characteristic impedance squared)
 - $Z_1 = j\omega L$ (series impedance)
 - $Z_2 = 1/j\omega C$ (shunt impedance)
2. Therefore:
 - $R_0^2 = Z_1 \times Z_2 = j\omega L \times 1/j\omega C = L/C$
 - $R_0 = \sqrt{L/C}$
3. Pass band condition:
 - $-1 < Z_1/4Z_2 < 0$
 - $-1 < j\omega L/(4 \times 1/j\omega C) < 0$
 - $-1 < -\omega^2 LC/4 < 0$
4. At cutoff frequency:
 - $\omega^2 LC/4 = 1$
 - $\omega C^2 = 4/LC$
 - $\omega C = 2/\sqrt{LC}$
 - $f_c = \omega C/2\pi = 1/\pi\sqrt{LC}$

Final Equation:

- Cutoff frequency $f_c = 1/\pi\sqrt{LC}$

Mnemonic: "KCLP: Konstant-k Cutoff in Low Pass depends on L and C product"